Multiply & Divide Integers Fact Sheet

A positive integer times a negative integer: A negative times a negative. Think of repeated addition here: $3 \times (-2) =$ $(-3) \times 3 =$ Complete the pattern on the $(-3) \times 2 =$ left. Observe how the products continually increase by 3 in $(-3) \times 1 =$ and and $(-3) \times 0 =$ each step. (-2)(-2)= -6. $(-3) \times (-1) =$ $(-3) \times (-2) =$ It follows that the *negative* Or, $4 \times (-7) = (-7) + (-7) + (-7) + (-7) = -28$. $(-3) \times (-3) =$ times negative products in the $(-3) \times (-4) =$ pattern must be positive. A positive integer times a negative integer: Another 'justification' for this rule can be seen Since you can change the order of the factors, using distributive property: $(-6) \times 4 = 4 \times (-6) = -24.$ Distributive property of arithmetic states that In general, if *m* and *n* are natural numbers, then a(b + c) = ab + ac. $m \times (-n)$ is (-n) added repeatedly m times, so is negative. And $(-m) \times n$ is the same as $n \times (-m)$ So, if a = (-1), b = 3, and c = (-3), it should still and so is negative as well. hold: (-1)(3 + (-3)) = (-1)(3) + (-1)(-3)both have a negative answer Now, since 3 + (-3) is zero, the whole left side is zero. So (-1)(3) + (-1)(-3) must be zero as well. Dividing a negative integer by a positive. (-1)(3) is -3. So it follows that (-1)(-3) has to Divide these negatives into be the opposite of -3, or 3. three equal groups. The 'negative times negative makes positive' $(-6) \div 3 = -2.$ rule has to do with the fact that IF we made it to Dividing a positive integer by a negative. be negative, then all these neat rules and properties of arithmetic wouldn't hold for What is $(-15) \div 5$? Let's call the answer Z. negative numbers. Since division and multiplication are opposite operations, $Z \times 5 = -15$. So Z must be -3. But mathematicians do want them to hold, since we DO want mathematics to be a very In general, if *m* and *n* are natural numbers, and consistent system. So the convention is made $(-m) \div n$ is B, then B × n = (-m), and B must be that negative times negative is positive. negative. Dividing a negative integer by a negative. In a nutshell, whether you multiply or divide: Let's say $(-21) \div (-7)$ is some number A. (different signs) yields a negative answer It follows that $A \times (-7) = (-21)$ Knowing the multiplication rules, the only number that fits A is 3. (same kind of signs) In general, if *m* and *n* are natural numbers, and vields a positive answer $(-m) \div (-n)$ is B, then B × (-n) = (-m), and B must be positive.